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# Anisotropy of acoustic and thermal expansion properties of TllnSe ${ }_{2}$ crystals 

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#### Abstract

Based on experimental studies of acoustic wave velocities in TllnSe ${ }_{2}$ crystals, all components of their elastic stiffness and compliance tensors are determined. $\mathrm{TllnSe}_{2}$ has three acoustic axes parallel to the principal crystallographic directions. The lowest velocities of acoustic eigenwaves are used to estimate the acousto-optic figure of merit. We analyse deviations from purely longitudinal and transverse polarization states, as well as the obliquity of acoustic energy flow. Temperature dependences of strains along the three principal crystallographic directions and of acoustic wave velocities $v_{11}, v_{22}$ and $v_{33}$ are measured. Anomalous behaviour of these parameters occur at $T_{1} C_{11}=C_{33} 245 \mathrm{~K}$ and $T_{2} C_{12}=C_{13} 145 \mathrm{~K}$. It is shown that the symmetry of TllnSe 2 becomes lower than tetragonal below the temperature point $T_{1}$.


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## 1. Introduction

TlInSe ${ }_{2}$ crystals belong to the group of ternary thallium halcogenides with a general formula $\mathrm{TlMX}_{2}$ ( $\mathrm{M}=\mathrm{Ga}, \mathrm{In} ; \mathrm{X}=\mathrm{Se}, \mathrm{S}, \mathrm{Te}$ ). They are characterized by layered or chain-like low-dimensional structures [1]. For instance, monoclinic $\mathrm{TlGaS}_{2}, \mathrm{TlInS}_{2}$ and $\mathrm{TlGaSe}_{2}$ have a layered structure [2-4], while tetragonal $\mathrm{TlGaTe} e_{2}, \mathrm{TlInTe} e_{2}$ and $\mathrm{TlInSe} e_{2}$ compounds crystallize in a chain structure [5]. Both types of crystals belong to the same group of $\mathrm{A}^{\mathrm{III}} \mathrm{B}^{\mathrm{II}} \mathrm{C}_{2}^{\mathrm{IV}}$ semiconductors. Most of the layered crystals of this family are proper ferroelectrics, with an incommensurate (IC) phase between the para and ordered phase. These crystals undergo phase transitions (PTs) with symmetry change $2 / \mathrm{m} \leftrightarrow$ IC $\leftrightarrow 2$ (see, e.g. the review [1]). However, the PTs are not fully understood. For example, it has been found that the layered $\mathrm{TlInS}_{2}$ crystals show metastable polytype structures and, as a result of polytypism, anomalies of their physical parameters appear at further temperatures. These anomalies correspond to various polytypes that are characterized by multiplication of the $c$ lattice parameter with $c=2 c^{\star}, 4 c^{\star}, 8 c^{\star}$ and $16 c^{\star}$, where $c^{\star}=15.18 \AA[6-10]$.

PTs are even more complex for chain-type tetragonal crystals. Using the studies of the heat capacity, the lattice parameters and the intensities of X-ray Bragg reflections, a second-order PT at 98.5 K has been detected in $\mathrm{TlGaTe}_{2}$ crystals [11] but not in other compounds in this group. Here the modulated IC structure has been assumed to exist at the temperatures above 98.5 K ( $110-290 \mathrm{~K}$ ). A number of temperature intervals with temperature independent lattice parameter a exist between 110 and 290 K . This behaviour has been explained as a so-called 'devil's staircase' [11]. $\mathrm{TlGaTe}_{2}$ has been studied down to temperatures of 5 K , with no additional PTs observed.

The existence of a non-ferroelectric PT at 98.5 K in $\mathrm{TlGaTe}_{2}$ has been confirmed by some other studies (see, e.g. [12,13]). As a result, several questions arise: (i) what is the nature of the phase below 98.5 K ? (ii) Is the phase above 98.5 K incommensurate or do different phases coexist in the temperature region $98.5-290 \mathrm{~K}$ ? (iii) What is the temperature of a para-to-IC PT, in case that the IC phase really exists?

PTs in TlInSe $e_{2}$ are even less clear. The authors of the study [14] have not found an anomaly in the heat capacity in the region $170-215 \mathrm{~K}$, although anomalies of the dielectric permittivity and the conductivity have reported at 210, 200 and 196.8 K [15]. Other $\mathrm{PTs}^{\text {in }} \mathrm{TlInSe}_{2}$ at 135 and 185 K were reported by Ref. [16] from the temperature dependence of the lattice parameter $a$. Alekperov et al. [17] reported anomalies at 135 and 185 K in the temperature dependence of the photoconductivity, the lattice parameter $a$, and the heat capacity of TlInSe ${ }_{2}$. They have suggested that the interval in between these points corresponds to the IC phase. The anomaly of the heat capacity at 185 K is more pronounced than the small diffused maximum observed at 135 K [17]. This does not agree with the fact that, usually, the para-to-IC PT and the IC-to-ordered PTs are of the second and first orders, respectively.

Although the X-ray studies of $\mathrm{TlInSe}_{2}$ have been carried out in several contributions, so-called satellite reflections corresponding to the superstructure have not been found ([18]), neither have they been found in [19]. However, Hosokawa et al. [19] have proposed an unusual concept of the IC phase. They suppose that the positions of Tl atoms fluctuate significantly with respect to the $\mathrm{InSe}_{4}$-chain framework in the IC phase existing above 135 K , although in the commensurate phase below 135 K , these atoms are located with corresponding distances well defined (about 0.34 nm ). This reflects a fact that the phase is perfectly ordered. According to [20], Tl atoms produce periodical one-dimensional arrays relative to In and $\mathrm{Se}_{2}$ layers in the para phase, and the periodicity becomes broken in the IC phase. On the other hand, no PT has been detected at 185 K in the work [19], although the authors of the study [20] believe that TlInSe ${ }_{2}$ should reveal a structural PT from the high-temperature normal phase into the IC phase at around 410-460 K, which coincides with the region where a giant thermoelectric effect appears [21].

Following from these contradictory data, one can conclude that the information available on the PTs in TlInSe $2_{2}$ is far from complete. The primary goal of our current work is to continue the studies of PTs in the TlInSe $2_{2}$ crystals. We include in our analysis the anisotropy appearing at the PTs, which should be accompanied by symmetry lowering of the properties under study, in particular, thermal expansion and acoustic wave (AW) velocities. Acoustic properties of TlInSe ${ }_{2}$ are also studied since the crystal seems to be a promising acousto-optic (AO) material. According to [22], the AO figure of merit (AOFM) for $\mathrm{TlInSe}{ }_{2}$ is equal to $156 \times 10^{-15} \mathrm{~s}^{3} / \mathrm{kg}$ at the wavelength $1.15 C_{44}=C_{66}=\left(C_{11}-C_{12}\right) / 2$ in the case of AO interactions with the longitudinal AW $v_{22}$. As shown in our recent work [23], the AOFM of $\mathrm{TlInS}_{2}$ can reach very high values, $\sim$ (2200$9000) \times 10^{-15} \mathrm{~s}^{3} / \mathrm{kg}$. This coefficient can increase at the interactions with slower quasi-transverse AWs. In order to analyse the anisotropy of AOFM [24-26], we determine complete matrices of elasto-optic and elastic-stiffness coefficients, which determine the AW velocities. Hence, below we also investigate the anisotropy of acoustic properties of the TlInSe ${ }_{2}$ crystals.

Let us remind in brief the main properties of TlInSe ${ }_{2}$, which are needed for our analysis. The TlinSe $e_{2}$ crystals belong to the space symmetry group $\mathrm{I} 4 / \mathrm{mcm}$ (point group $4 / \mathrm{mmm}$ ). Their lattice parameters are $a=8.075 \AA$ and $c=6.847 \AA(Z=4)$ [5]. TlInSe ${ }_{2}$ exhibits a giant Peltier-Seebeck effect below 410 K , with the Seebeck coefficient being as high as $10^{5}-10^{7} \mu \mathrm{~V} / \mathrm{K}$ at room temperature. It is believed to be related to the IC structure of these crystals [20]. The crystal is transparent in the infrared spectral range at the wavelengths longer than $\sim 1 \mu \mathrm{~m}$ (the bandgap $E_{g}=1.18 \mathrm{eV}$ at 300 K ) [27]. For the best of our knowledge, the data for the low-energy absorption edge is not available in the literature. The temperature dependence of the linear thermal expansion coefficient has earlier been studied [28]. However, the experimental geometry and, in particular, the orientation of the sample with respect to the crystallographic coordinate system was not given [28] so that comparison with our data is difficult. The refractive indices were studied with an ellipsometric technique [29].

Using a standard Sellmeier approximation and the data reported in [29], we have calculated the refractive indices at $1.15 \mu \mathrm{~m}: n_{o}=2.99$ and $n_{e}=3.26$.

## 2. Experimental techniques and procedures

To synthesize and grow the ternary compound $\mathrm{TlInSe}{ }_{2}$ using initial substances of high purity. The synthesis was performed using standard melting methods. The TlInSe $e_{2}$ crystals were grown with a Bridgman-Stockbarger technique at the Institute of Electronic Physics of NAS of Ukraine. The initial substances were loaded into quartz ampoules with the inner diameter of $15-20 \mathrm{~mm}$. They were soldered after reaching the vacuum $10^{-4} \mathrm{~mm} \mathrm{Hg}$. The melt of the TlInSe $2_{2}$ compound was crystallized along a horizontal direction. The temperatures were $800-840^{\circ} \mathrm{C}$ in the melting zone and $690-710^{\circ} \mathrm{C}$ in the annealing zone. The melting temperature of $\mathrm{TlInSe}_{2}$ is $750^{\circ} \mathrm{C}$. The vertical temperature gradient in the zone of crystallization was $3-5^{\circ} \mathrm{C} / \mathrm{mm}$ and the velocity at which the ampoule moved from the melting zone to the annealing zone was $0.10-0.25 \mathrm{~mm} / \mathrm{h}$. The crystals in Figure 1 were cooled at the rate of $50-60^{\circ} \mathrm{C} / \mathrm{h}$. The crystal structure was checked by X-ray diffraction. Our data agreed well with the results in [5]. The directions of the crystallographic axes were determined using the same X-ray method.

The relative thermal expansions $\Delta L_{i} / L_{j}^{0}=\left(L_{i}-L_{i}^{0}\right) / L_{j}^{0}$ (with $L_{i}^{0}$ and $L_{j}^{0}$ being the initial sizes of a sample respectively along the directions $i$ and $j$, and $L_{i}$ the thermally induced size) were measured with a quartz-capacity dilatometer along the crystallographic axes $a, b$ and $c$. The thermal expansion tensor $\alpha_{i j}=\partial\left(\Delta L_{i} / L_{j}^{0}\right) / \partial T$ for the tetragonal TIInSe ${ }_{2}$ crystals written in the crystallographic coordinate system is as follows:

$$
\alpha_{i j}=\left|\begin{array}{ccc}
\alpha_{a a} & 0 & 0  \tag{1}\\
0 & \alpha_{b b} & 0 \\
0 & 0 & \alpha_{c c}
\end{array}\right|,
$$

where $\alpha_{b b}=\alpha_{a a}$. The volume thermal expansion coefficient was determined as $\alpha_{V}=\alpha_{a a}+\alpha_{b b}+\alpha_{c c}$. The dilatometer was built at the Vlokh Institute of Physical Optics (Lviv, Ukraine). The average sensitivity of our dilatometer was about 2 nm in the region $105-300 \mathrm{~K}$ under test. The measurements were carried out in the cooling run, with the temperature scan rate $0.02 \mathrm{~K} / \mathrm{min}$. The accuracy of temperature measurements was not worse than 0.01 K . The meansquare error for the thermal expansion coefficients did not exceed $\sim 0.7 \times 10^{-5} \mathrm{~K}^{-1}$. The samples for the thermal expansion measurements had the same size as those prepared for the AW-velocity measurements (see below).

We prepared three nearly cubic-shaped samples of $\mathrm{TIInSe}_{2}$ for the AW velocity measurements. The faces of these samples were perpendicular respectively to (1) $a, b$ and $c$ axes, (2) $b$ axis, and directions [101] and [10 $\overline{1}]$, and (3) $c$ axis, and directions [110] and [1 $\overline{1} 0]$. The average dimensions of our samples were $\sim 5 \times 5 \times 5 \mathrm{~mm}^{3}$. The AW velocities were measured with the error $<2 \%$ using a pulse echo-overlap method [30]. We excited the AWs by standard $\mathrm{LiNbO}_{3}$ transducers with the resonance frequency $f=10 \mathrm{MHz}$, the bandwidth $\Delta f=0.1 \mathrm{MHz}$ and the acoustic power $P_{a}=1-2 \mathrm{~W}$. The


Figure 1. TllnSe ${ }_{2}$ crystals grown in the present work.

AW velocities were denoted using the indices associated with the crystallographic axes, according to the standard notation $a=1, b=2$ and $c=3$.

The elastic-stiffness coefficients were calculated using the AW velocities determined experimentally and the formulae $C_{11}=\rho v_{11}^{2}, C_{33}=\rho v_{33}^{2}, C_{44}=\rho v_{23}^{2}, C_{66}=\rho v_{12}^{2}, C_{12}=2\left(\rho v_{66}^{2}-C_{66}\right)-C_{11}$ and $C_{13}=\sqrt{\left(C_{11}-2 \rho v_{55}^{2}+C_{44}\right)\left(C_{33}-2 \rho v_{55}^{2}+C_{44}\right)}-C_{44}$. Here $\rho=6460 \mathrm{~kg} / \mathrm{m}^{3}$ is the material density determined by us, and $v_{i j}$ the AW velocities (with $i$ and $j$ indicating respectively the propagation and polarization directions of the AW). The elastic compliances were calculated, following from the matrix of elastic-stiffness coefficients and the formulae

$$
\begin{align*}
& S_{11}=S_{22}=\frac{C_{11} C_{33}-C_{13}^{2}}{C_{33} C_{11}^{2}-2 C_{13}^{2} C_{11}-C_{12}^{2} C_{33}+2 C_{13}^{2} C_{12}}, \quad S_{33}=\frac{C_{11}+C_{12}}{C_{11} C_{33}-2 C_{13}^{2}+C_{12} C_{33}}, \\
& S_{12}=\frac{C_{13}^{2}-C_{12} C_{33}}{C_{33} C_{11}^{2}-2 C_{13}^{2} C_{11}-C_{12}^{2} C_{33}+2 C_{13}^{2} C_{12}}, \quad S_{13}=S_{23}=-\frac{C_{13}}{C_{11} C_{33}-2 C_{13}^{2}+C_{12} C_{33}},  \tag{2}\\
& S_{55}=S_{44}=1 / C_{44}, \quad S_{66}=1 / C_{66} .
\end{align*}
$$

The obliquity angle between the acoustic group-velocity direction and the AW vector was calculated using the relation [31]

$$
\begin{equation*}
\Delta_{i}=\arctan \frac{1}{v\left(\phi_{i}\right)} \frac{\partial v\left(\phi_{i}\right)}{\partial \phi_{i}} \tag{3}
\end{equation*}
$$

$v\left(\phi_{i}\right)$ denotes a function of AW velocity that depends upon the angle $\phi_{i}$ between the wave vector and the corresponding axis of the crystallographic coordinate system, with the subscript $i$ referring to the axis perpendicular to the geometric plane under consideration.

The angle of deviation of the AW polarization from purely longitudinal types is also a very important characteristic of AO materials. We calculated this angle from the Christoffel equation [32]:

$$
\begin{align*}
& \zeta_{1}=\frac{1}{2} \arctan \frac{\left(C_{13}+C_{44}\right) \sin 2 \phi_{1}}{\left(C_{11}-C_{44}\right) \cos ^{2} \phi_{1}+\left(C_{44}-C_{33}\right) \sin ^{2} \phi_{1}}  \tag{4}\\
& \zeta_{3}=\frac{1}{2} \arctan \frac{\left(C_{11}+C_{66}\right) \sin 2 \phi_{3}}{\left(C_{11}-C_{66}\right) \cos ^{2} \phi_{3}+\left(C_{66}-C_{11}\right) \sin ^{2} \phi_{3}} \tag{5}
\end{align*}
$$

These relations refer respectively to the $b c$ and $a b$ planes. Here $\phi_{1}\left(\right.$ or $\left.\phi_{3}\right)$ is the angle between the AW vector and the $b$ (or $a$ ) axis. The corresponding non-orthogonality of quasi-transverse (QT) waves can be calculated in the same manner, with the only difference that the additive factor of $90^{\circ}$ should be added to the r.h.s. of formulae (4) and (5).

For all the data presented in the following figures, the error bars are less or comparable with the diameter of the data points.

## 3. Results and discussion

### 3.1. Acoustic and elastic anisotropy

The AW velocities are listed in Table 1. The velocities of quasi-longitudinal (QL) waves are moderate. For QT waves are the velocities of the AWs propagating along the principal crystallographic axes do not exceed $1356 \mathrm{~m} / \mathrm{s}$. These velocities predispose high AOFM for TlInSe ${ }_{2}$, which is proportional to the inverse cube of the AW velocity. Based on the AW velocities determined experimentally, we

Table 1. AW velocities measured for $\mathrm{TllnSe}_{2}$.

| $i j$ | 11 | 33 | 55 | 66 | 12 | 23 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $v_{i j}(\mathrm{~m} / \mathrm{s})$ | $2553 \pm 25\left(v_{11}=v_{22}\right)$ | $3596 \pm 30$ | $2838 \pm 25$ | $2444 \pm 20$ | $1319 \pm 12\left(v_{12}=v_{21}\right)$ | $1356 \pm 15$ |

have calculated a complete matrix of elastic-stiffness coefficients. Table 2 lists also the elastic-compliance coefficients. One can see that the $S_{44}$ and $S_{66}$ coefficients are larger than the other tensor components. This means that the TlInSe ${ }_{2}$ crystals are very compliant with respect to the shear stresses $\sigma_{4}$, $\sigma_{5}$ and $\sigma_{6}$.

Using the matrix of elastic-stiffness coefficients, we construct the cross sections of the AW velocity surfaces by the principal crystallographic planes. In the bc plane, only the velocity of the AW $\mathrm{QT}_{1}$ does not depend on the propagation direction (see Figure 2(a)). As seen from Figure 2(b), all the acoustic eigenwaves manifest no significant anisotropy in the $a b$ plane. The lowest velocity for the

Table 2. Elastic-stiffness and compliance coefficients calculated for $\mathrm{TllnSe}_{2}$.

| $i j$ | 11 | 33 | 12 | 13 | 44 | 66 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $C_{i j}\left(10^{9} \mathrm{~N} / \mathrm{m}^{2}\right)$ | $42.11 \pm 0.45$ | $83.54 \pm 0.69$ | $12.59 \pm 0.98$ | $8.93 \pm 1.61$ | $11.88 \pm 0.22$ | $11.24 \pm 0.21$ |
| $S_{i j}\left(10^{-12} \mathrm{~m}^{2} / \mathrm{N}\right)$ | $26.41 \pm 0.53$ | $12.40 \pm 0.19$ | $-7.47 \pm 0.77$ | $-2.03 \pm 0.39$ | $84.19 \pm 1.52$ | $88.98 \pm 1.69$ |




Figure 2. Cross sections of AW velocity surfaces by the crystallographic planes $b c$ (a) and $a b$ (b), as calculated for TIInSe $e_{2}$ : $e$ denotes the displacement vector.

QL waves, $2444 \mathrm{~m} / \mathrm{s}$, is reached in the case when the AW propagates along bisector between the $a$ and $b$ axes (Figure 2(b)). The lowest velocity for the $\mathrm{QT}_{1}$ and $\mathrm{QT}_{2}$ waves is equal to $1356 \mathrm{~m} / \mathrm{s}$ when the $\mathrm{QT}_{1}$ wave propagates along arbitrary directions inside the $b c$ plane (Figure 2(a)), or when the $\mathrm{QT}_{2}$ wave propagates in any direction inside the $a b$ plane (Figure 2(b)) or along the $c$ axis (Figure 2(a)). The crystallographic axes $a, b$ and $c$ represent the acoustic axes for the transverse AWs. Under propagation along these directions, the velocities of transverse eigenwaves are the same (see Figure 2). Thus, $\mathrm{TlInSe}{ }_{2}$ has three acoustic axes under normal conditions.

As seen from Figure 3(a), the obliquity angle for the $\mathrm{QT}_{2}$ and QL waves acquires high enough values in the $b c$ plane. This angle is $40.7^{\circ}$ when the wave vector of the $\mathrm{AW} \mathrm{QT}_{2}$ makes the angle $18^{\circ}$ with respect to the $b$ axis. When the orientation angle of the QL wave vector is $45^{\circ}$ with respect to the $b$ axis in the $b c$ plane, the obliquity angle is $28.6^{\circ}$. The obliquity angles for the $\mathrm{QT}_{1}$ waves do not exceed $1.5^{\circ}$ in this plane. At the same time, the $\mathrm{AW} \mathrm{QT}_{1}$ is characterized by large obliquity in the $a b$ plane (see Figure 3(b)). Consequently, we have $\pm 15.2^{\circ}$ at the wave vector orientations given by the angles $23^{\circ}$ and $69^{\circ}$ with respect to the $a$ axis. Finally, the obliquity angles for the QL waves in the


Figure 3. Dependences of obliquity angle of AW energy propagation on the direction of AW vector in the $b c$ (a) and $a b$ (b) planes, as calculated for $\mathrm{TllnSe}_{2}$.
$a b$ plane are quite small $\left(\sim 5.0^{\circ}\right)$ and the effect in this plane is completely absent for the $\mathrm{AW}_{\mathrm{QT}}^{2}$ (see Figure 3(b)).

As seen from Figure 4(a), the angle of deviation from the purely transverse or longitudinal polarization states in the $b c$ plane reaches the value $22.8^{\circ}$ when the AW vector is oriented under the angle $48^{\circ}$ with respect to the $b$ axis in the $b c$ plane (the cases of the $\mathrm{AWs} \mathrm{QT}_{2}$ and QL). It is equal to $\pm 7.7^{\circ}$ when the AW vector is oriented under the angles $19^{\circ}$ or $71^{\circ}$ with respect to the $a$ axis in the $a b$ plane (the cases of the AWs $\mathrm{QT}_{2}$ and QL - see Figure 4(b)).

The angle of deviation from the purely transverse or longitudinal polarization states and the obliquity angle are a measure of crystal anisotropy. For example, in a so-called isotropic approximation ( $C_{11}=C_{33}, C_{12}=C_{13}$ and $\left.C_{44}=C_{66}=\left(C_{11}-C_{12}\right) / 2\right)$ it follows from Equations (4) and (5) that the angle of deviation from the purely transverse or longitudinal polarization states vanishes. The same concerns the obliquity angle defined by a general relation given by Equation (3).

The temperature dependences of the AW velocities $v_{11}, v_{22}$ and $v_{33}$ and the appropriate elasticstiffness coefficients $C_{11}, C_{22}$ and $C_{33}$ are shown in Figure $5(\mathrm{a}, \mathrm{b})$, respectively. We find $C_{11}=C_{22}$


Figure 4. Dependences of the angle of deviation from purely transverse and longitudinal polarization states on the direction of AW vector in $\mathrm{TllnSe}_{2}$, as calculated for the AWs QL and $\mathrm{QT}_{2}$ in the $b c$ plane (a) and for the AWs QL and $\mathrm{QT}_{1}$ in the $a b$ plane (b).
for crystals belonging to the tetragonal point symmetry group $4 / \mathrm{mmm}$ but not so for crystals of lower-symmetry systems, e.g. the orthorhombic. At temperatures below ca. 270 K , the temperature curves for the AW velocities and the elastic-stiffness coefficients are split, and a small break of these curves is observed at $T_{1} \approx 245 \mathrm{~K}$ (see Figure $5(\mathrm{a}, \mathrm{b})$ ). The measurements of the AW velocities in the temperature region below $166-185 \mathrm{~K}$ become difficult due to scattering of the AWs and disappearing of the reflected signal. This can be caused by diffusion of the phase transition in the vicinity of $T_{2^{-}}$ $\approx 145 \mathrm{~K}$, with the appearance of phase coexistence and nucleation of a domain structure. The reflected signal has not been clearly detected down to the lowest temperature of our measurements near 120 K .

Unfortunately, the data for the elasto-optic coefficients of $\mathrm{TlInSe}_{2}$ are not available in the literature. Nevertheless, one can take the AOFM data from Ref. [22] ( $\left.M_{2}=156 \times 10^{-15} \mathrm{~s}^{3} / \mathrm{kg}\right)$ and determine the component $p_{11}=p_{22}$ of the elasto-optic tensor from the formula $\left|p_{22}\right|=\sqrt{M_{2} v_{22}^{3} \rho / n_{o}^{6}}$. This AOFM value corresponds to the isotropic AO interaction with the longitudinal AW that propagates along the $b$ axis (type 1 of AO interactions - see Figure 6). We find $\left|p_{22}\right|=0.15$ for the optical wavelength $1.15 \mu \mathrm{~m}$. As mentioned above, the slowest AW QL propagates along the bisector of the $a$ and $b$ axes. One of the possible isotropic interactions with this AW, which corresponds to the type 2 of AO interactions, is shown in Figure 6. Neglecting a small Bragg angle, we write the effective elasto-optic coefficient for this interaction type as $p_{e f}=\left(p_{11}+p_{12}+2 p_{66}\right) / 2$. Using the isotropic approximation and assuming that $p_{66} \approx\left(p_{11}-p_{12}\right) / 2$ we obtain $p_{e f} \approx p_{11}$. In this case, we derive


Figure 5. Temperature dependences of AW velocities $v_{11}, v_{22}$ and $v_{33}$ (a) and elastic-stiffness coefficients $C_{11}, C_{22}$ and $C_{33}$ (b) for TllnSe ${ }_{2}$ crystals.


Figure 6. Schematic wave vector diagram for isotropic AO interactions with the AWs QL propagating along the $b$ axis (1) and along bisector of the $a$ and $b$ axes in the $a b$ plane. $k_{i}$ and $k_{d}$ denote the wave vectors of incident and diffracted optical waves, whereas $K_{a c}$ is the AW vector. Double-sided arrows and crossed circles indicate polarizations of the optical waves.
a somewhat higher AOFM ( $M_{2} \approx 170 \times 10^{-15} \mathrm{~s}^{3} / \mathrm{kg}$ ), which is due to the increased slowness of the QL wave. However, one needs to know all of elasto-optic tensor components in order to perform a more reliable analysis of the AOFM anisotropy.

### 3.2. Thermal expansion anisotropy

The behaviour of the relative linear elongation (Figure 7(a)) and the volume thermal expansion (Figure $7(\mathrm{~b})$ ) are notably changed below $T_{1} \approx 245 \mathrm{~K}$ under cooling. This temperature is far removed from 185 K , which could be associated with the PT in the light of the earlier literature data. Nonetheless, it does follow from the temperature dependence of the lattice parameter $a$ [17] that, with decreasing temperature, the lattice parameter in the vicinity of $T_{1}$ starts to deviate from a linear trend, in spite of the fact that the heat capacity measured in the same work reveals the anomaly at 185 K . The temperature curves of the relative elongations along the $a$ and $b$ axes are split at $T_{1}$ (see Figure 7(a)), thus indicating that the crystal symmetry becomes lower and corresponds to one of the orthorhombic symmetry groups.

However, a comparison of Figure $7(\mathrm{a}, \mathrm{b})$ shows that a temperature decrease below $T_{1}$ leads to expansion along all of the three principal axes, which manifests itself in differences between the dashed lines and the experimental points corresponding to spontaneous strains. This fact is unusual for ferroic crystals where the PTs are accompanied by lattice strains since the trace of the spontaneous strain tensor should be equal to zero [33] avoiding changes of the unit-cell volume. In fact, we have observed a change of the volume expansion at $T_{1}$ (see Figure 7(b)), which is given by a difference of the dashed line and the data represented by experimental points. Notice also that the volume thermal expansion is almost independent of temperature between the points $T_{1}$ and $T_{2} \approx 145 \mathrm{~K}$ (i.e. the volume thermal expansion coefficient is equal to zero - see Figure 8(b)), although the sample starts to expand sharply below $T_{2}$.

The linear thermal expansion coefficients at $T=290 \mathrm{~K}$ are equal to $\alpha_{a a}=(3.3 \pm 0.7) \times 10^{-5} \mathrm{~K}^{-1}$, $\alpha_{b b}=(2.3 \pm 0.7) \times 10^{-5} \mathrm{~K}^{-1}$ and $\alpha_{c c}=(0.4 \pm 0.7) \times 10^{-5} \mathrm{~K}^{-1}$ (see Figure 8(a)). Taking the experimental errors into account, we conclude that the components $\alpha_{a a}$ and $\alpha_{b b}$ are equal to each


Figure 7. Temperature dependences of relative linear elongation (a) and volume thermal expansion (b) for $\mathrm{TllnSe}_{2}$. Dashed lines correspond to linear extrapolation from the region $T>245 \mathrm{~K}$.
other both at the normal conditions and above the temperature point $T_{1}$. However, the linear thermal expansion curves $\alpha_{a a}$ and $\alpha_{b b}$ are split as the temperature decreases below $T_{1}$. Below $T_{2}$, the linear thermal expansion coefficients and the volume thermal expansion coefficient (see Figure 8(b)) become negative and increase in modulus almost two orders of magnitude. Such an abrupt variation of these parameters testifies some structural changes that occur below the temperature point $T_{2}$, as well as a lowered symmetry of $\mathrm{TlInSe} \mathrm{e}_{2}$ below $T_{1}$.

## 4. Conclusions

Based on the comprehensive studies of the AW velocities, we have determined all components of the elastic-stiffness and compliance tensors for TlInSe ${ }_{2}$ crystals. It has been found that the elastic compliances $S_{44}=S_{55}$ and $S_{66}$ are much larger than other tensor components, thus testifying an extremely high compliance of TlInSe $2_{2}$ with respect to shear stresses. Using the cross sections of the AW velocity surfaces, we have found that TlInSe $2_{2}$ contains three acoustic axes parallel to the principal crystallographic directions. The lowest velocities of the acoustic eigenwaves have been determined. The lowest velocity for the QL waves, $2444 \mathrm{~m} / \mathrm{s}$, is reached when the AW propagates along the bisector of the


Figure 8. Temperature dependences of linear (a) and volume (b) thermal expansion coefficients for $\mathrm{TllnSe}_{2}$.
$a$ and $b$ axes. The lowest velocity for the $\mathrm{QT}_{1}$ and $\mathrm{QT}_{2}$ waves is equal to $1356 \mathrm{~m} / \mathrm{s}$. It corresponds to the $\mathrm{QT}_{1}$ wave propagating along arbitrary direction inside the $b c$ plane, as well as the $\mathrm{QT}_{2}$ wave propagating in any direction in the $a b$ plane, or along the $c$ axis. The AOFM has been estimated for the case of AO interactions with the slowest QL wave. It has been shown that the angle between the direction of the acoustic energy flow and the AW vector in $\mathrm{TlInSe}{ }_{2}$ is high enough. The same is true of the angle of deviation of AW polarization from the purely longitudinal or transverse states.

We have studied the temperature behaviour of the relative elongation along the three principal crystallographic directions. The corresponding dependences of the thermal expansion coefficients have been obtained. The linear thermal expansion coefficients at $T=290 \mathrm{~K}$ are equal to $\alpha_{a a}=(3.3 \pm 0.7) \times 10^{-5} \mathrm{~K}^{-1}, \alpha_{b b}=(2.3 \pm 0.7) \times 10^{-5} \mathrm{~K}^{-1}$ and $\alpha_{c c}=(0.4 \pm 0.7) \times 10^{-5} \mathrm{~K}^{-1}$. Anomalous behaviour of these parameters has been detected at $T_{1} \approx 245 \mathrm{~K}$ and $T_{2} \approx 145 \mathrm{~K}$. Unfortunately, we cannot make clear conclusions on the origin of structural changes that appear at the $T_{1}$ and $T_{2}$ points in TlInSe ${ }_{2}$ basing on the results presented in this study. Nonetheless, following from the temperature dependences of the AW velocities and the thermal expansion data, we conclude that the symmetry of $\mathrm{TlInSe}_{2}$ becomes lower than tetragonal one below the $T_{1}$ point. Along with the appearance of spontaneous strains along the principal crystallographic directions, this can point to a ferroelastic nature of the PT. Moreover, there can be phase coexistence in the
temperature region between the $T_{1}$ and $T_{2}$ points. Notice that a specific temperature point $T_{2} \approx 145 \mathrm{~K}$ is detected close to the temperature $T=135 \mathrm{~K}$ where the phase transition from the IC phase to the ordered phase has been detected [17-21]. The point $T_{1} \approx 245 \mathrm{~K}$ may correspond to the temperature 185 K supposed to be at a PT [17]. Increased scattering of the AWs has been found at 185 K . As follows from the smooth anomalies of AW velocities, the AW scattering, the relative elongation and the thermal expansion coefficients measured in the present work, we conclude that $\mathrm{TlInSe}_{2}$ undergoes several phase transitions and passes through a wide temperature range of phase coexisting.

## Disclosure statement

No potential conflict of interest was reported by the authors.

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